Hydrodynamic coefficients of oscillating flat plates at $0.15 \leq KC \leq 3.15$

Xinliang Tian$^{1,2}$ · Longbin Tao$^{1,3}$ · Xin Li$^{1,2}$ · Jianmin Yang$^{1,2}$

Received: 26 January 2016 / Accepted: 21 May 2016 © JASNAOE 2016

Abstract This article presents an experimental investigation on the hydrodynamic coefficients of oscillating flat plates. The plates are forced to oscillate harmonically in still water. The range of Keulegan–Carpenter number ($KC = \frac{2\pi a}{D}$, where $a$ is the single amplitude of oscillation and $D$ is the equivalent diameter of the plate) is $0.15 \leq KC \leq 3.15$. The hydrodynamic forces acting on the plates are measured and the hydrodynamic coefficients including added mass and damping coefficients are calculated using the Morison’s equation. The influences of the thickness ratio, shape, edge corner radius, perforation ratio and hole size on the hydrodynamic coefficients of a single plate are analyzed and presented. For the twin- and triplet-plate configurations, the spacing effects are also evaluated.

Keywords Flat plate · Oscillatory flow · Added mass · Damping

1 Introduction

Floating offshore structures at sea may experience motion responses due to the incident wave forces. The amplitude of heave motion is a particular concern for engineers, because large heave motion may cause damages in risers, drilling pipes and onboard equipments. There are two ways to minimize the heave motion responses, either adjusting the natural heave period of the platform and making it out of the wave frequency region to avoid resonance, or increasing the heave damping of the system. For the deepwater Spar platform, heave plates are usually installed at the bottom of the platforms and have been demonstrated to be effective devices to improve the heave motion performance [2]. This is because the heave plates significantly increase the effective heave added mass of the platform, and the natural period of the heave motion is increased and moved further out of the wave-period region. Furthermore, the heave plates enhance the vortex shedding pattern and increase the damping of the system. Therefore, the added mass and damping are considered as the main parameters characterizing the hydrodynamic performance of the heave plates.

For a rigid body oscillating in a fluid at rest or a fixed body in an oscillatory flow, Keulegan–Carpenter number ($KC$) and the Reynolds number are, respectively, defined as

$$KC = \frac{2\pi a}{D}$$
$$Re = \frac{U_{\text{max}}D}{v}$$

where $D$ is the characteristic dimension of the body, e.g., diameter for a circular disk, $a$ is the single amplitude of the oscillation, $U_{\text{max}}$ is the maximum velocity of the oscillation and taken as $U_{\text{max}} = (KC)D/T$, $T$ is the period of the oscillation and $v$ is the kinematic viscosity of the fluid. The frequency number $\beta$ given by the ratio of $Re$ and $KC$ is also used in this study, so that

$$\beta = \frac{Re}{KC} = \frac{D^2}{vT}$$
Many experimental (see, e.g., [3, 5, 6, 9, 13, 17, 18]) and numerical (see, e.g., [4, 7, 8, 11, 12, 14–16, 19]) investigations on the hydrodynamic performance of heave plates have been conducted in the past two decades. The added mass and damping of the heave plates are dependent on both $KC$ and $\beta$. The effects of geometric configurations are also investigated, e.g., the size of the plates [17], the distances between multiple plates [6, 7, 14], the thickness [3, 6, 15–17], the porosity [6, 8, 13] and the edge taper angles [11]. The effect of the plate shape have not been considered.

It is noted that the previous studies were mainly focused on the cases at low $KC$ numbers, i.e., $KC \leq 1.2$. The hydrodynamic characteristics of the oscillating flat plates at higher $KC$ number are required to be addressed. In the present study, we carried out a forced oscillation test for the flat plates at $0.15 \leq KC \leq 3.15$ using a self-developed motion mechanism. The range of $KC$ is decided by the upper and lower limits of the present experimental setup for reliable measurement. The effects of thickness ratios, shapes, edge corner radii, perforation ratio and perforated hole size as well as the spacing between multiple plates on the hydrodynamic coefficients of plates are also investigated.

## 2 Experimental apparatus

The experiments were carried out in the State Key Laboratory of Ocean Engineering in Shanghai Jiao Tong University. Figure 1 shows the physical photo and the schematic diagram of the test facility which was carefully designed for the oscillation tests. The main dimension of the test facility is 1.5 m long, 1.1 m wide and 3.0 m high. The facility consists of the main frame, the motion mechanism and the observation water tank.

The main frame is made of steel with sufficient stiffness and weight, ensuring that structural vibration is eliminated during the oscillation test. As shown in Fig. 1, the crank-slider mechanism is used to generate the one-dimensional oscillatory motion. The crank is driven by a servo motor. The period of oscillation is determined by the rotation speed of the crank and the oscillation amplitude is determined by the radius of the crank.

The rail and the supporting lines ensure that the rod and heave plate oscillate in through the center of the plate. Therefore, one-dimensional oscillation could be generated with various amplitudes and periods. The linkage is as long as 1.2 m and the maximal radius of the crank is 0.1 m, ensuring that the oscillation motion of the plate is approximately harmonic.

The axial force on the rod is measured by a tension/compression type load cell. The rated capacity of the load cell is 200 N and the nonlinearity of the load cell is within 0.5% of the rated output. The rod may also provide damping forces to the system due to its interactions with the water and the supporting lines. Oscillation tests without plate show that the damping force provided by the rod is very small compared with the damping force provided by the plate; therefore, the effect of the rod on the damping of the system is neglected. The motion of the heave plate is recorded with a laser displacement sensor. The accuracy of the displacement sensor is within 0.01 mm. The sampling frequency of the measurement is 100 Hz. As the synchronization of the motion and force measurements is crucial to the added mass and damping results, the phase lag between the motion and force signals are measured carefully before the formal oscillation tests. The phase lag is kept within 0.01 s, which is no more than 2% of the period of the oscillation motion.

The main dimensions of the water tank are 1 m long, 1 m wide and 1.1 m deep. The depth of the water is 1 m and the mean position of the plate is at 0.5 m below the water surface. The ratio of the dimension of the tank and the diameter of plates is about five which is close to the value in the configurations used by [3] and [13]. For the oscillation tests with large amplitudes, the influences of the free surface should be carefully considered. According to the experimental results by [6], the influence of immersion depth of the plate could be negligible when the immersion depth was larger than one diameter of the plate. In the present study, the minimal distance between the plate and free surface was more than two times of the diameter of the plate. Furthermore, there was no evident free surface elevation in any test. Thus, the effects of the
The matrix for the single plate test is shown in Table 2, Table 1 shows the parameters for the plate models used for the oscillation test.

### 3 Plate models

The influences of the thickness ratio, shape, edge corner radius, perforation ratio, hole size and the spacing between multiple plates on the hydrodynamic coefficients of oscillating plates are considered. It is not practical to do the test for all the different combinations of the considered factors. Therefore, seven individual sets of comparison test are designed for investigating the influences of the seven different factors, respectively. A circular flat plate model with a diameter of 200 mm is used as a basic plate shape for comparing. Table 1 shows the parameters for the plate models used for the oscillation test.

The sets A–E are designed for evaluating the influences of thickness ratio, plate shape, edge corner radius, perforation ratio and hole size, respectively. Additionally, to investigate the spacing effect of the multiple plates, the sets F and G are designed for the twin- and triplet-plate tests, respectively. In this study, twin- and triplet-plate configurations are considered. In Fig. 3, the plate model A2 is used in model tests for multiple plates. In this study, twin- and triplet-plate configurations are considered for investigating the spacing effects, see the multiple-plate models in Fig. 3.

### 4 Test matrix

The matrix for the single plate test is shown in Table 2, where \( \uparrow \) and \( \times \) refer to the cases carried out and not, respectively. 37 runs of oscillation tests are conducted for each single plate model and the \( KC \) number ranges from 0.15 to 3.15. For each \( KC \) number, two or three oscillation frequencies are selected, i.e., \( f = 1, 1.5 \) and 2 Hz, respectively. Thus, the corresponding frequency number is \( b = (4 \sim 8) \times 10^4 \). The choice of these parameters ensures that the measured force is within the optimal working region of the load transducer, and also ensures that there is no evident water surface elevation during the tests. Each test runs at least 30 cycles, and at least 15 cycles in the "steady state" will be used for the data processing.

### 5 Hydrodynamic force coefficients

Disregarding the friction between the supporting wires and the rod, the motion equation of the rod and the plate model could be written as

\[
M \ddot{z} = F_{\text{rod}} + F_{\text{byc}} - Mg
\]  

(4)

where \( M \) is the total mass of the plate and rod; \( \ddot{z} \) is the acceleration of plate which is calculated by second derivative of the plate motion \( z \); \( g \) is the acceleration of gravity; \( F_{\text{rod}} \) is the hydrodynamic force acting on the plate and rod; \( F_{\text{byc}} \) is the force measured by the force transducer installed at the top end of the rod; \( F_{\text{byc}} \) is the buoyancy of the plate and the rod. It is noted that \( F_{\text{rod}} \) could be written as the sum of the static component \( (F_{\text{rod}}^s) \) and the dynamic component \( (F_{\text{rod}}^d) \), i.e., \( F_{\text{rod}} = F_{\text{rod}}^s + F_{\text{rod}}^d \). \( F_{\text{byc}} \) could also be written as the sum of the static component \( (F_{\text{byc}}^s) \) and the dynamic component \( (F_{\text{byc}}^d) \), i.e., \( F_{\text{byc}} = F_{\text{byc}}^s + F_{\text{byc}}^d \). \( F_{\text{rod}}^d \) accounts for the variation of the buoyancy during oscillation. \( F_{\text{byc}}^d \) can be calculated as \( F_{\text{byc}}^d = -\rho g A_{rod} \ddot{z} \), where \( A_{rod} \) is the area of the cross section of the rod. Therefore, according to Eq. 4, the hydrodynamic force \( F_{\text{rod}} \) is calculated as

\[
F_{\text{rod}} = M \ddot{z} - F_{\text{rod}} - F_{\text{byc}} + Mg
\]  

(5)

\[
= M \ddot{z} - (F_{\text{rod}}^s + F_{\text{rod}}^d) - (F_{\text{byc}}^s - \rho g A_{rod} \ddot{z}) + Mg
\]  

(6)

In the static state (the disk is submerged in water but without oscillation), the force measured at the top of the rod \( (F_{\text{rod}}^s) \) equals to the difference between the gravity \( (Mg) \) and buoyancy \( (F_{\text{byc}}^s) \) of the rod and plate. Therefore, we have

\[
Mg - F_{\text{rod}}^s - F_{\text{byc}}^s = 0.
\]

Equation 6 could be rewritten as

\[
F_{\text{rod}} = M \ddot{z} - F_{\text{rod}}^d + \rho g A_{rod} \ddot{z}
\]  

(7)

The hydrodynamic force acting on the rod is neglected because it is very small compared with the hydrodynamic force acting on the plate. Therefore, \( F_{\text{rod}} \) is considered as the hydrodynamic force acting on the flat plate. The hydrodynamic damping force on the plate \( (F_d) \) can be expressed using a quadratic representation (Morison’s equation), as follows:
\[ F_d(t) = C_d \frac{1}{2} \rho \frac{\pi D^2}{4} \hat{z}\hat{\tau} \]  

(8)

where \( C_d \) is the drag coefficient and \( \hat{z} \) is the velocity of the plate. Since the plate is forced to oscillate sinusoidally, the drag coefficient and added mass coefficient (\( C_a \)) are calculated using Fourier analysis, respectively, as [10]

\[ C_d = -\frac{3\omega}{\rho n U_{\text{max}}^2} \int_0^T F_{\text{hyd}}(t) \cos(\omega t) \, dt \]  

(9)
**Fig. 2** Photo of the flat plate models

(a) plates A1–A12

(b) plates B1–B8

(c) plates C1–C4

(d) plates D1–D4

(e) plates E1–E5

**Fig. 3** Photo of the multiple-plate models

(a) twin-plate (F2)

(b) triplet-plate (G2)
where $\omega$ is the circular frequency and taken as $\omega = 2\pi/T$, $C_a$ is the added mass coefficient, $\forall$ is the immersed volume of the plate, taken as $\forall = (1/4)\pi D^2 t_d$, and $\rho$ is the density of the fluid.

The hydrodynamic drag force can also be expressed using an equivalent linear damping coefficient $B$ as

$$F_d(t) = B \dot{z}$$

The two coefficients $B$ and $C_d$ can be related to each other by the equivalent linearization of the quadratic damping using Fourier decomposition [10], thus

$$B = \frac{1}{3} \sqrt{\frac{\rho \beta D(KC)}{C_d}}$$

For the convenience of comparing the results with previous studies, the added mass and the damping coefficients are further nondimensionalised against the theoretical ideal fluid added mass, $m' = (1/3)\rho D^3$. Thus, the added mass and damping coefficients are rewritten, respectively, as

$$A' = \frac{C_a m}{m'}$$

$$B' = \frac{B}{2m'\omega} = \frac{(KC)C_d}{4\pi}$$

where $m$ is the displacement mass of the disk, $m = \rho \forall$.

## 6 Results and discussions

The characteristics of damping and added mass of the plates could be represented by either $C_d$ and $C_a$ or $B'$ and $A'$, respectively. $B'$ and $A'$ are used in this study for the convenience of comparing the results with [3] and [13]. For each heave plate, 37 tests are conducted and 37 sets of $A'$ and $B'$ results are obtained, respectively. As the effect of frequency ($\beta$) on the hydrodynamic results is actually weak [3], the results of $A'$ and $B'$ are only plotted against $KC$ in this study. Because there are many data points in each comparable test set, it is not feasible to plot all the data points of different plates together. Therefore, to provide a clear comparison of the results of different plates, the results for each plate are fitted using a quadratic polynomial regression, see Fig. 4 as an example. The coefficient of determination denoted as $R^2$ is introduced to evaluate how well data fit the regression line. The value of $R^2$ ranges from 0 to 1. An $R^2$ of 1 indicates that the regression line perfectly fits the data, while an $R^2$ of 0 indicates that the line does not fit the data at all. The values of $R^2$ for the different plates are all above 0.96, indicating a favorable representation of the experimental results. The original data points are available online as the electronic supplementary material.

### 6.1 Comparison with the literatures

To validate the present experimental setup and measurements, the added mass and damping coefficients of the plates A1, A2 and A4 are compared with the experimental results by [3] and [13], see Fig. 5. It should be noted that, as there lack cases with exactly the same parameters from different studies, only some of the most similar cases are selected for comparison.

As shown in Fig. 5a, a relative large scatter is observed in the results of the added mass coefficients from different experimental studies. However, the monotonous relation between $A'$ and $KC$ is clearly indicated in each case. For the plate of $t_d/D = 0.02$, the added mass coefficient obtained from the present test at $\beta = (4 \sim 8) \times 10^4$ agrees well with...
the results by [13] at $\beta = 8 \times 10^4$. Compared with the results of the added mass coefficient by [3], the results of the present study is generally higher for the plate of $t_d/D = 0.01$ and is generally lower for the plate of $t_d/D = 0.04$. As shown in Fig. 5b, a good agreement is observed in the damping coefficients between the present study and [13]. Compared with the results by [3], for the plates with similar/same thickness ratio, the damping coefficients obtained in the present study are higher. As we know, for the lightly damped system, the inertia force dominates the total force experienced by the system. Therefore, it is difficult to identify the damping force in the total force measured. Different experimental configurations often give different damping results. There are several reasons that may affect the damping coefficient. First of all, the phase lag between displacement and force signals is essential for the calculation of the damping coefficient, as indicated in Eqs. 9 and 10. On the other hand, experimental investigations by [1] demonstrate that the damping of the submerged oscillating plate may be affected by the free surface. Thus, the influences of free surface should be carefully checked. However, it is noted that both the present study and the study by [3] have successfully revealed the trend that the damping coefficient decreases as the plate thickness of the plate increases for the thin plates.

For the thin plate oscillating perpendicular to its plane in a fluid, the force acting on the disk is dominated by the pressure drag (form drag) rather than the friction drag. On the other hand, the flow separation point is always fixed at the plate tips. Thus, it has been widely recognized that the effect of frequency (or Reynolds number) on this problem is very weak. However, it is noted in Fig. 5 that the added mass and damping coefficients in the work of [13] have shown some discrepancies between the results at different frequencies. As we know, for a given oscillating amplitude, the total force acting on the disk is approximately proportional to the square of frequency, i.e., $F \propto f^2$. In the work of [13], the considered oscillating frequency ranges from 0.1 Hz to 1 Hz, it implies that the magnitude of the force acting on the disk at the low frequency (0.1 Hz) is about two orders smaller than that at the high frequency (1 Hz). That means the load cell must keep a very good accuracy in a very wide measurement range. It is normally not easy to achieve this. Based on our experience, the optimal working range of the load cell used in the present study is suggested to be within 30–70% of the maximal measurement range of the load cell. In the present study, the abandon of the test case at $f = 1$ Hz, $a = 5$ mm (see Table 2) is because the magnitude of the measured force is very small with respect to the measurement range of the load cell.

6.2 Influences of thickness ratio

Figure 6 shows the variations of the added mass ($A'$) and damping coefficient ($B'$) of the plates with different thickness ratios with respect to $KC$. The range of thickness ratio ($t_d/D$) considered here is from 0.01 to 0.4. As shown in Fig. 6a, for all the considered thickness ratios, $A'$ increases as $KC$ increases. The thinnest plate $A_1$ among the 12 plates provides the highest value of $B'$. Similar to the feature of $A'$, the influences of thickness ratio on $B'$ is more significant in the high $KC$ region than that in the low $KC$ region. Figure 6b shows the results of $B'$ for the plates with different thickness ratios. As shown in Fig. 6b, the damping coefficient $B'$ increases as $KC$ increases for all the considered thickness ratios. The thinnest plate $A_1$ among the 12 plates provides the highest value of $B'$. Similar to the feature of $A'$, the influences of thickness ratio on $B'$ is more significant in the high $KC$ region than that in the low $KC$ region. [15] investigated the flow regimes around an oscillating plate with a sharp edge based on the axis-symmetric numerical simulations, and three vortex shedding patterns, i.e., independent, interactive and unidirectional, are observed. The mechanism of the flow
regime is found to be dependent on the thickness ratio of the disk and KC number. As shown in Fig. 6, a large range of thickness ratio is investigated here; therefore, it is not easy to obtain a representative conclusion on the influence of thickness ratio on the added mass and damping coefficient of plates. It is noted that the results of $A_0$ for the plates A1–A8 follow one similar trend while the results of $A_0$ for the rest plates follow the other similar trend. For the damping coefficient $B_0$, the results of plates A1–A6 follow one similar trend while the results for the rest plates follow the other similar trend. Therefore, it appears that the variation features of $A_0$ and $B_0$ with respect to KC should be discussed, respectively, for the “thick” and “thin” plates. Based on the experimental results shown in Fig. 6, the critical value of the thickness ratio for defining the “thick” and “thin” plates is between 0.05 and 0.075. Generally, for the “thin” plates, $A_0$ decreases as the thickness ratio increases; for the “thick” plates, the influence of thickness ratio on $B_0$ is not significant. It is noted that the plate A1 which is the thinnest plate in the 12 test plates provides the maximum damping. This is consistent with the finding by [16] that the thinner plate could provide more damping.

6.3 Influences of plate shape

Figure 7 shows the variations of the added mass ($A'$) and damping coefficient ($B'$) of the plates with different shapes with respect to KC. For visual convenience, the geometry of the plates (plates B1–B8 in Table 1) is included in Fig. 7. Eight typical plate shapes are considered here, i.e., circular (B1), octagon (B2), hexagon (B3), square (B4), triangle (B8) and three rectangle plates with different width/length ratios (B5–7). As shown in Fig. 7a, except the rectangle plates B6 and B7, $A'$ for the rest plates increases.
as $KC$ increases. It appears that the results of $A'$ for the circular (B1), octagon (B2) and hexagon (B3) plates are very close, while $A'$ for the rest plates is lower than that for the plates B1–B3. For the rectangle plates, $A'$ decreases as the width/length ratio of the plate decreases. It is concluded that the fully filled shapes like circular, octagon and hexagon could provide more added mass than the less filled shapes. As shown in Fig. 7b, $B'$ of the plates with different shapes are very close in the region of $KC \lesssim 2.5$. It appears that the influence of shape on the damping coefficient is not as significant as that on the added mass.

### 6.4 Influences of edge corner

Figure 8 shows the results of the added mass coefficient ($A'$) and damping coefficient ($B'$) of the plates with different edge corner radii with respect to $KC$. Here, the plate models are the circular plate with a thickness of 10 mm and a diameter of 200 mm, giving a thickness ratio of 0.05. According to the discussion in Sect. 6.2, the plates are the “thin” plates. Apart from the sharp edge plate C1, the edges of rest three plates C2–C4 are rounded with different radii, i.e., $r = 1, 3, 5$ mm, respectively. As shown in Fig. 8a, the effect of corner radius on $A'$ is significant, i.e., the plate with sharper edges provide more added mass. As shown in Fig. 8b, for the cases at $KC < 1$, the influence of edge corners on $B'$ is not significant; for the cases at $KC > 1$, the sharper the plate edge is, the higher $B'$ is.

### 6.5 Influences of porosity

In this section, the influences of porosity on the hydrodynamic coefficients of the plates are considered. Here, we evaluate two parameters, i.e., the porosity ratio and the perforated hole size.

#### 6.5.1 Influences of porosity ratio

Figure 9 shows the results of the added mass coefficient ($A'$) and damping coefficient ($B'$) of the plates with
different porosity ratios at different $KC$. As shown in Fig. 9a, $A'$ decreases significantly as the porosity ratio increases. The added mass coefficient for the plate with 20% porosity is about 40%–60% lower than that for the solid plate. As shown in Fig. 9b, for the cases at low $KC$ numbers, i.e. $KC \leq 0.6$, the perforated plates appear to provide more damping compared with the solid plate, and the perforated plate with medium porosity (around 10%) would provide the highest damping. However, for the cases at $KC \geq 0.75$, the solid plate provides more damping.

It is noted that the results of $A'$ and $B'$ in Fig. 9 are calculated using the nominal area ($A$) of the perforated plates, rather than the actual area. In Fig. 10, the force coefficients are recalculated using the actual area of the plates. As shown in Fig. 10a, even based on the actual area of the plate, the added mass coefficient still decreases as the porosity ratio of the plate increases. However, as shown in Fig. 10b, for the damping coefficient calculated based on the actual area of the plate, the damping coefficient increases as the porosity ratio increases for a given $KC$.

6.5.2 Influences of perforated hole size

Figure 11 shows the results of the added mass coefficient ($A'$) and damping coefficient ($B'$) of the plates with different perforated hole sizes. The five plate models considered here are of the same porosity ratio 10%. As shown in Fig. 11, the influences of perforated hole size on the added mass and damping coefficients are not significant. It appears that the added mass coefficient of a perforated plate is mainly dominated by the porosity ratio rather than the hole size.

6.6 Influences of plate spacing

In this section, we consider the configuration of multiple plates arranged in axial alignment. In this case, the hydrodynamic coefficients may be influenced by the spacing between the plates, which is denoted as $l$. Limited by the capacity of the test facilities, the twin-plate and triplet-plate configurations are considered here, respectively. The
influences of $l$ on the added mass and damping coefficients of the plates are investigated.

6.6.1 Twin-plate configurations

Figure 12 shows the influences of the spacing between twin plates on the added mass coefficient ($A'$) and damping coefficient ($B'$) at different $KC$ numbers. For the convenience of comparing the hydrodynamic coefficients of twin plates with those of a single plate, the results of the single plate is also plotted in Fig. 12. Moreover, the line denoted by “Single plate × 2” in Fig. 12 represents the results of the single plate magnified by a factor of two. As shown in Fig. 12a, $A'$ of the twin plates increases as $KC$ increases. However, compared with the single plate, the added mass coefficient of the twin plate is not doubled. It is strange to find that, when the spacing is very small (e.g., $l/D = 0.075, 0.145$), the added mass coefficient of twin plates at a large $KC$ number is lower than that of the single plate. This is because the hydrodynamic characteristics of the twin plates with very small spacing is similar to those of a thick plate. It has been concluded in Fig. 6a that, in large $KC$ number regions, $A'$ of a “thick plate” is generally lower than that of a “thin plate”. As shown in Fig. 12a, as $l$ increases, the twin plates are no longer be treated as a “thick plate”. The influences of the thickness ratio start to give way to the influences of the plate–plate interactions. The added mass of twin plates appears to increase as the spacing between the plates increases. It is noted that for the spacing as large as $l/D = 0.755$, the deduction effect of multi-plate interactions still exists, even though $A'$ of the twin plates has been significantly increased compared with the single plate. As shown in Fig. 12b, the influences of $l$ on $B'$ for the twin-plate configuration is similar to that on $A'$. The damping coefficient of twin plates at small spacings is close to that of a single thick plate. For the large spacing configurations, the suppression effect of the multiple plates decreases as the spacing increases. It is interesting to note that, compared with the case $l/D = 0.145$, $B'$ of the configuration $l/D = 0.075$ is lower in the region of $KC < 1.2$ and higher in the region of $KC > 1.2$. This is because that, in the low $KC$ region, the interaction between multiple plates is relatively weak and the damping coefficient of twin plates increases as the spacing increases. However, as $KC$ increases, the hydrodynamic characteristics of the twin plates become approximately equivalent to that of a single thick plate. Therefore, the smaller the spacing $l$ is, the larger the damping coefficient $B'$ is.

6.6.2 Triplet-plate configurations

Figure 13 shows the influences of the spacing between triplet plates on the added mass coefficient ($A'$) and damping coefficient ($B'$) at different $KC$ numbers. Similar to Fig. 12 for the twin-plate configuration, the results of the single plate are also shown in Fig. 13. Moreover, the line denoted by “Single plate × 3” in Fig. 13 represents the results of the single plate magnified by a factor of three. Due to the limitation of the test tank size, the maximum spacing for the triple plates is $l/D = 0.3975$. As shown in Fig. 13a, for the small spacing configuration ($l/D = 0.075$), the result of $A'$ is lower than that of a single plate in the low $KC$ region, and is higher that of a single plate in the high $KC$ region. Similarly, as shown in Fig. 13a, $B'$ of the triplet plates at small $l$ configurations is lower than that of a single plate. Moreover, as $l$ increases, the interaction between the triplet plates becomes weaker, the added mass and damping coefficients of the triplet plates increases.
Conclusions

The hydrodynamic characteristics of an isolated plate with different geometries are investigated with a forced oscillation test. The KC number considered here is in the range of $0.15 \leq KC \leq 3.15$. The influences of thickness ratio, shape, edge corner, porosity ratio and the perforated hole size on the added mass ($A'$) and damping ($B'$) coefficients of the plate are evaluated. Moreover, the influences of the spacing between multiple plates are also investigated with the twin-plate and triplet-plate configurations, respectively. The main conclusions are drawn as follows:

- The variation features of $A'$ and $B'$ with respect to $KC$ should be discussed, respectively, for the “thick” and “thin” plates. The critical value of the thickness ratio for defining the “thick” and “thin” plates is between 0.05 and 0.075. For the “thin” plates, $A'$ decreases as the thickness ratio increases; for the “thick” plates, $A'$ increases as the thickness ratio increases. The “thick” plates provide more added mass in the region of $KC \leq 0.5$ while the “thin” plates provide more added mass in the region of $KC \geq 0.5$. For the “thin” plates, $B'$ decreases as the thickness ratio increases; for the “thick” plates, the influence of thickness ratio on $B'$ is not significant.
- The nearly fully filled shapes like circular, octagon and hexagon could provide more added mass than the less filled shapes. The influence of shape on the damping coefficient is not as significant as that on the added mass.
- $A'$ and $B'$ are influenced by the edge corner of the plates. The plate with sharp edges could provide more added mass and damping than the plates with round corners.
- The added mass of the plate decreases with the porosity of the plate. The medium porosity (around 10%) could provide more damping when $KC \lesssim 0.6$, and the solid plate provides more damping when $KC > 0.75$. The damping coefficient calculated based on the actual area of plate increases as the porosity increases for a given $KC$. For a given porosity ratio, the influences of the perforated hole size on $A'$ and $B'$ are not significant.
- The added mass and damping of the multiple-plate configurations are significantly influenced by the spacing between the plates. The configuration of the plates with a small spacing is approximately equivalent to the case of a single thick plate. For the configurations with a large spacing, the interaction between multiple plates becomes weaker as the spacing increases.

In summary, the influences of various geometry factors on the hydrodynamic characteristics of oscillating plates are investigated via a forced oscillation test. The conclusions drawn here and the data presented in this paper are of significance for the engineering applications of flat plates. However, it should be noted that the tests in this study were carried out only for the isolated plates. In engineering applications, the hydrodynamic coefficients of heave plates may also be influenced by some other factors, such as the large structural components near the heave plate and free surface effect. Therefore, in case of the heave plate installed close to the column of platform or free surface, the experimental data presented in this study are not applicable. Additional investigations should be carried out to evaluate the influence of these factors.

Acknowledgments This work was supported by the Shanghai Yang Fan Program (Grant No. 15YP1406100), the National Natural Science Foundation of China (Grant No. 51509152) and the Newton Research Collaboration Programme (Grant No. NRCP/1415/211).
References